# POLARIZED STRUCTURE FUNCTIONS AT A NEUTRINO FACTORY

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## **Q:** WHAT IS A $\nu$ FACT GOOD FOR?

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THE CHORUS TARGET

## ... INTO THIS MAGNET



THE COMPASS TARGET MAGNET

## THE CERN NEUTRINO FACTORY DESIGN

MUON BEAM ENERGY	$E_{\mu} = 50  { m GeV}$
LENGTH OF THE STRAIGHT SECTION	L = 100  m
DISTANCE OF DETECTOR FROM END OF THE STRAIGHT SECT	N. $d = 30 \text{ m}$
NR. OF $\mu$ decays per yr. along the straight sectn.	$N_{\mu}=10^{20}$
MUON BEAM ANGULAR DIVERGENCE	$0.1 imes m_\mu/E_\mu$
MUON BEAM TRANSVERSE SIZE	$\sigma_x = \sigma_y = 1.2 \text{ mm}$
PROTON TARGET RADIUS (DIS)	$R = 50 { m ~cm}$
PROTON TARGET RADIUS (ELASTIC)	$R = 20 { m ~cm}$
PROTON TARGET EFF. DENSITY (UNPOL. TARGETS)	$100 \mathrm{~gr/cm^2}$
PROTON TARGET EFF. DENSITY (POL. TARGETS)	$10 \mathrm{~gr/cm^2}$

NUTEV, CHORUS: ~  $10^6$  events;  $E_{\nu} = 10 \div 200$  GeV CHORUS,  $E_{\nu} = 20 \div 400$  GeV NuTeV



## **PHYSICS MOTIVATIONS**

See M. L. Mangano et al. hep-ph/0105155; I. Bigi et al., hep-ph/0106177

#### • NEUTRINO OSCILLATIONS:

- Observation of all three oscillations
- Determination of  $\theta_{13}$  &  $\delta m_{13}$
- CP violation in neutrino mixing

#### • **PRECISION PHYSICS:**

- EW parameters  $(\sin^2 \theta_W, \text{ CKM matrix elements}, ...)$
- strong coupling constant  $(\alpha_s)$
- parton distributions of the nucleon

#### • PROCESSES HITHERTO UNOBSERVED IN CC SECTOR:

- polarized charged-current DIS: S.F., Mangano, Ridolfi, N.P. B602 (2001) 585
- charm factory physics
- $\nu$ -induced nuclear effects

#### • EXOTICA:

- $-\nu e$  annihilation, neutrino structure functions
- skewed parton distributions
- new physics

## **D.I.S. WITH PARITY VIOLATION**

#### STRUCTURE FUNCTIONS...



Lepton fractional energy loss:  $y = \frac{p \cdot q}{p \cdot k}$ ; Bjorken x:  $x = \frac{Q^2}{2p \cdot q}$ lepton-nucleon CM energy:  $s = \frac{Q^2}{xy}$ ; virtual boson-nucleon CM energy  $W^2 = Q^2 \frac{1-x}{x}$ ;

$$\frac{d^2 \sigma^{\lambda_p \lambda_\ell}(x, y, Q^2)}{dx dy} = \frac{G_F^2}{2\pi (1 + Q^2/m_W^2)^2} \frac{Q^2}{xy} \left\{ \left[ -\lambda_\ell y \left( 1 - \frac{y}{2} \right) x F_3(x, Q^2) + (1 - y) F_2(x, Q^2) \right. \right. \\ \left. + y^2 x F_1(x, Q^2) \right] - 2\lambda_p \left[ -\lambda_\ell y (2 - y) x q_1(x, Q^2) - (1 - y) q_4(x, Q^2) - y^2 x q_5(x, Q^2) \right] \right\}$$

$-y^2 x F_1(x,Q^2)$	$-2\lambda_p$	$\left\lfloor -\lambda_{\ell} y(2 - \lambda_{\ell}) \right\rfloor$	$y)x \mathbf{g_1}($	$(x,Q^2) -$	(1 -	$(y)g_4(x,Q^2)$	$-y^2 x g_5$	$\left[ \left( x,Q^{2} ight)  ight] $
								J

		PARITY CONS.	PARITY VIOL.
$\lambda_l \rightarrow $ lepton helicity	UNPOL.	$F_1$ , $F_2$	$F_3$
$\lambda_p \rightarrow \text{proton helicity}$	POL.	$g_1$	$g_4$ , $g_5$

#### **PARTON DISTRIBUTIONS**

STRUCTURE FUNCTION=HARD COEFF. ©PARTON DISTN.



$$F_2^{\mathrm{NC}}(x,Q^2) = x \sum_{\text{flav. }i} e_i^2(q_i + \bar{q}_i) + \alpha_s \left[C_i[\alpha_s] \otimes (q_i + \bar{q}_i) + C_g[\alpha_s]\right]$$

 $q_i$  quark,  $\bar{q}_i$  antiquark, g gluon

**LEADING PARTON CONTENT** (up to  $O[\alpha_s]$  corrections)

$$q_{i} \equiv q_{i}^{\uparrow\uparrow} + q_{i}^{\uparrow\downarrow} \qquad \Delta q_{i} \equiv q_{i}^{\uparrow\uparrow} - q_{i}^{\uparrow\downarrow}$$

$$NC \qquad F_{1}^{\gamma, Z} = \sum_{i} e_{i}^{2} (q_{i} + \bar{q}_{i}) \qquad g_{1}^{\gamma, Z} = \sum_{i} e_{i}^{2} (\Delta q_{i} + \Delta \bar{q}_{i})$$

$$CC \qquad F_{1}^{W^{+}} = \bar{u} + d + s + \bar{c} \qquad g_{1}^{W^{+}} = \Delta \bar{u} + \Delta d + \Delta s + \Delta \bar{c}$$

$$CC \qquad -F_{3}^{W^{+}}/2 = \bar{u} - d - s + \bar{c} \qquad g_{5}^{W^{+}} = \Delta \bar{u} - \Delta d - \Delta s + \Delta \bar{c}$$

$$F_{2} = 2xF_{1} \qquad g_{4} = 2xg_{5}$$

 $W^+ \to W^- \Rightarrow u \leftrightarrow d, c \leftrightarrow s$ ; more combinations using Isospin:  $p \to n \Rightarrow u \leftrightarrow d$ 

## FLAVOUR SEPARATION





• CAN DISENTANGLE INDIVIDUAL PDFS BY LINEAR COMBINATION: AT LO

$$\frac{1}{2} \left( g_1^{W^-} - g_5^{W^-} \right) = \Delta u + \Delta c; \qquad \qquad \frac{1}{2} \left( g_1^{W^+} + g_5^{W^+} \right) = \Delta \bar{u} + \Delta \bar{c} \\ \frac{1}{2} \left( g_1^{W^+} - g_5^{W^+} \right) = \Delta d + \Delta s; \qquad \qquad \frac{1}{2} \left( g_1^{W^-} + g_5^{W^-} \right) = \Delta \bar{d} + \Delta \bar{s}$$

 $\Delta c, \Delta \bar{c}, \Delta s, \Delta \bar{s}$  only present above charm threshold

#### STRUCTURE FUNCTIONS AT THE $\nu$ FACTORY: UNPOLARIZED...

#### EVENT RATES

(DEFAULT BEAM AND DETECTOR)

**EXPECTED STAT. ERRORS** 



KINEMATIC COVERAGE AND ACCURACY RATHER BETTER THAN CURRENT CHARGED LEPTON EXPERIMENTS (E.G. NMC)

#### ...AND POLARIZED

![](_page_11_Figure_1.jpeg)

#### STATISTICAL ACCURACY ABOUT ONE ORDER OF MAGNITUDE BETTER THAN CURRENT POLARIZED CHARGED-LEPTON EXPERIMENTS!

#### POLARIZED PARTON DISTRIBUTIONS: WHAT DO WE KNOW?

![](_page_12_Figure_1.jpeg)

WORLD DATA (SMC, 1999)

FIRST MOMENTS

- QUARK ISOTRIPLET:  $\Delta q_3(1) = 1.11 \pm 0.04$ ;
- SCALE-INV. QUARK SINGLET:  $\Delta \Sigma(1) = 0.38 \pm 0.03;$
- GLUON:  $\Delta g(1, 1 \,\mathrm{GeV}^2) = 0.8 \pm 0.2;$

[Altarelli, Ball, S.F., Ridolfi, 1998-2001] stat. errors only; main syst: small x/shape

Note: quark SU(3) octet from  $\beta$  decays only;  $\Delta q_8(1) = 0.6 \pm 0.2(?)$ 

- FIRST MOMENTS KNOWN BETTER THAN SHAPES: TRIPLET ACCURATE, QUARK SINGLET AVERAGE; GLUON SEMI-QUANTITATIVE
- SHAPES KNOWN VERY POORLY
- ONLY SINGLET/TRIPLET FLAVOUR SEPARATION POSSIBLE
- CANNOT DISENTANGLE QUARK FROM ANTIQUARK

#### **A THEORETICAL CONSTRAINT: POSITIVITY**

**POSITIVITY OF CROSS SECTION REQUIRES**  $|\Delta q \leq q$ ,  $|\Delta \bar{q} \leq \bar{q}$ (up to small, computable NL correction [Altarelli, S.F., Ridolfi, 1998])

![](_page_13_Figure_2.jpeg)

unpolarized pdfs: CTEQ5+Barone et al. (strange); polarized pdfs: ABFR

- UP, DOWN: ANTIQUARK << QUARK ( $\Delta \bar{u} \approx \Delta \bar{d} \approx 0$ )
- STRANGE: ANTIQUARK CAN BE LARGE OR SMALL  $(\Delta \bar{s} \approx \Delta s \text{ or } \Delta \bar{s} \approx 0 \text{ both allowed})$

#### THE SPIN PUZZLE

AXIAL CHARGES (for flavor i):  $\langle N; p, s | J_{5,i}^{\mu} | N; p, s \rangle = a_i M_N s^{\mu}$ SINGLET AXIAL CHARGE  $\Rightarrow$  QUARK SPIN FRACTION (??)

$$a_0 \equiv \sum_{i=1}^{n_f} a_i = \int_0^1 dx \, \sum_{i=1}^{n_f} \left( \Delta q_i + \Delta \bar{q}_i \right) + O(\alpha_s)$$

EXPECT  $a_0 \approx a_8 \equiv \Delta u + \Delta d - 2\Delta s$  (Zweig Rule  $\rightarrow$  Ellis-Jaffe Sum Rule) GET  $a_0 = 0.10 \substack{+0.17 \\ -0.11}$  ( $Q^2 = \infty$ ) VS.  $a_8 = 0.58 \pm 0.03$  [ $\pm 30\%$  SU(3) violn. (?)]

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#### **SCENARIOS**

Define a scale-independent quark (by choice of facn. scheme):

$$a_0 = \int_0^1 dx \, \sum_{i=1}^{n_f} \left( \Delta q_i + \Delta \bar{q}_i \right) - \frac{\alpha_s}{2\pi} \int_0^1 dx \, \Delta g$$

- ANOMALY:  $\frac{\alpha_s}{2\pi} \int_0^1 dx \,\Delta g \approx a_0 a_8$ , Zweig Rule Respected by Scale-invariant quark first moment
- INSTANTON:  $\frac{\alpha_s}{2\pi} \int_0^1 dx \, \Delta g \ll a_8$ , SCALE-INVARIANT QUARK  $\approx a_0 \approx 0$  effect can be induced by QCD vacuum on sea quarks (instantons)
- SKYRMION:  $\Delta u_v + \Delta d_v = -\Delta s_v$ , SMALL POLARIZATION OF VALENCE QUARKS hence unrelated to glue, happens in Skyrme or chiral models

### WHAT WOULD WE LIKE TO KNOW?

IS THE GLUON CONTRIBUTION "LARGE"? (w.r. to quark) IF NOT, REFUTE THE ANOMALY SCENARIO IS THE SCALE–INVARIANT QUARK "SMALL"? (w.r. to octet) IF NOT, REFUTE THE INSTANTON SCENARIO

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## What would we learn at a $\nu$ fact ?

- ASSUME THE VALIDITY OF A SCENARIO & FIT TO CURRENT DATA
- GENERATE PSEUDO-DATA WITH REALISTIC ERRORS AND BINNING FOR A NUFACT
- REFIT TO CURRENT + PSEUDODATA

LIGHT FLAVOUR SEPARATION:

- Present: Triplet  $a_3 = 1.11 \pm 0.04$ ; no info on  $\Delta q \Delta \bar{q}$
- $\nu$ -FACT.:  $a_3 = 1.107 \pm 0.006$ ;  $\Delta(u \bar{u}) = 0.764 \pm 0.006$ ;  $\Delta(d \bar{d}) = -0.320 \pm 0.008$

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CAN EASILY TELL SCENARIOS FROM EACH OTHER BUT ERROR ON SINGLET DRIVEN BY ERROR ON GLUON: ONLY OBSTACLE TO FULL UNDERSTANDING OF SPIN STRUCTURE IS  $\Delta g!$ 

#### ... WHAT ABOUT SHAPES?

![](_page_23_Figure_1.jpeg)

## MORE...

- CHARM FACTORY PHYSICS: CHARM PRODUCED IN  $W^+ + s \rightarrow c$ easily tagged through dimuon signal, 2nd muon from subsequent c decay (Gehrmann)  $\Rightarrow$  STRANGE QUARK
- $\Lambda$  POLARIZATION IN THE CURRENT FRAGMENTATION REGION  $\Rightarrow$  FRAGMENTATION FUNCTIONS (Anselmino et al.)
- $\nu$ -INDUCED EXCLUSIVE  $D_s$  PRODUCTION  $\Rightarrow$  GENERALIZED PARTON DISTRIBUTIONS (Lehmann-Dronke and Schäfer)

#### 0.01 c) 0 $\xi \Delta s (\xi, \mu^2)^{\mu^2 = 22 \text{ GeV}^2}$ -0.01 0.01 0 $\mu^2 = 13 \text{ GeV}^2$ -0.01 0.01 0 $\mu^2 = 8 \text{ GeV}^2$ -0.01 0.01 gluon 0 $\mu^2 = 5 \text{ GeV}^2$ -0.01 0.01 0 $\mu^2 = 3.5 \, \text{GeV}^2$ -0.01 10 -2 10<sup>-1</sup> - 1

ξ

#### AN EXAMPLE: POLARIZED STRANGENESS

Strange distn. at LO directly determined by tagged-charm structure function:

$$g_{1,c}^{W^+}(x,Q^2) = |V_{cs}|^2 \Delta s(\xi,\mu_c^2) + |V_{cd}|^2 \Delta d(\xi,\mu_c^2);$$

$$\xi = x(1+m_c^2/Q^2);\, \mu_c^2 = Q^2 + m_c^2$$

Statistical errors small; however large error induced by QCD corrns. due to uncertainty on gluon

EXCELLENT DETERMINATION OF SHAPE IF GLUON KNOWN (COMPASS, RHIC...)

# CONCLUSIONS

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15 YEARS DOWN THE ROAD!