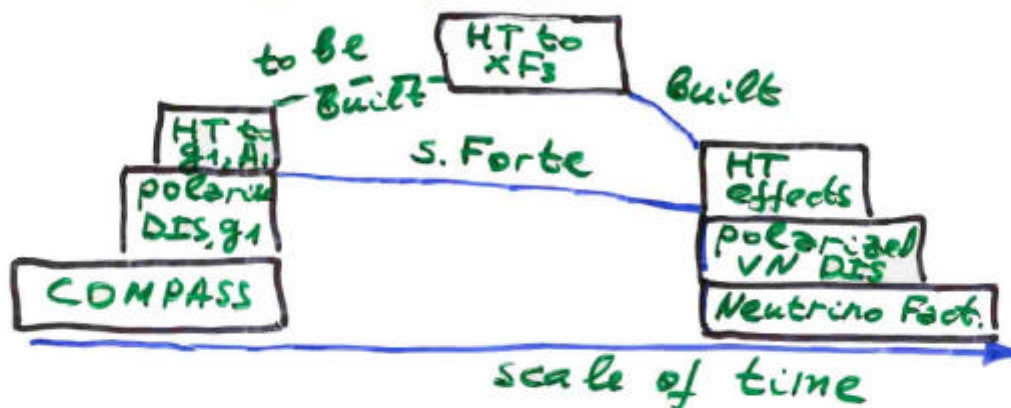


① Higher twists to  $xF_3$  as the part of the bridge between COMPASS and Neutrino Factory.

A. L. Kataev

INR, Moscow



Plan

① What is Neutrino Factory

M. Mangano et al (01)

② HT to  $xF_3$ : what do we know at NLO, NNLO and Beyond

Kataev, Kotikov, Parente, Sidorov (98)

Kataev, Parente, Sidorov (01)

③ HT contributions to  $A_1 \approx (1+\gamma^2) \frac{g_1}{F_1}$ ;  $\gamma^2 = \frac{4M_N^2}{Q^2}$   
start of the study at NLO

Leader, Sidorov, Stamenov (00)

Are there any relations



④ Conclusion



## ECFA STUDIES -> END 2000

### A Neutrino Factory Complex

#### Physics opportunities at the neutrino factory:

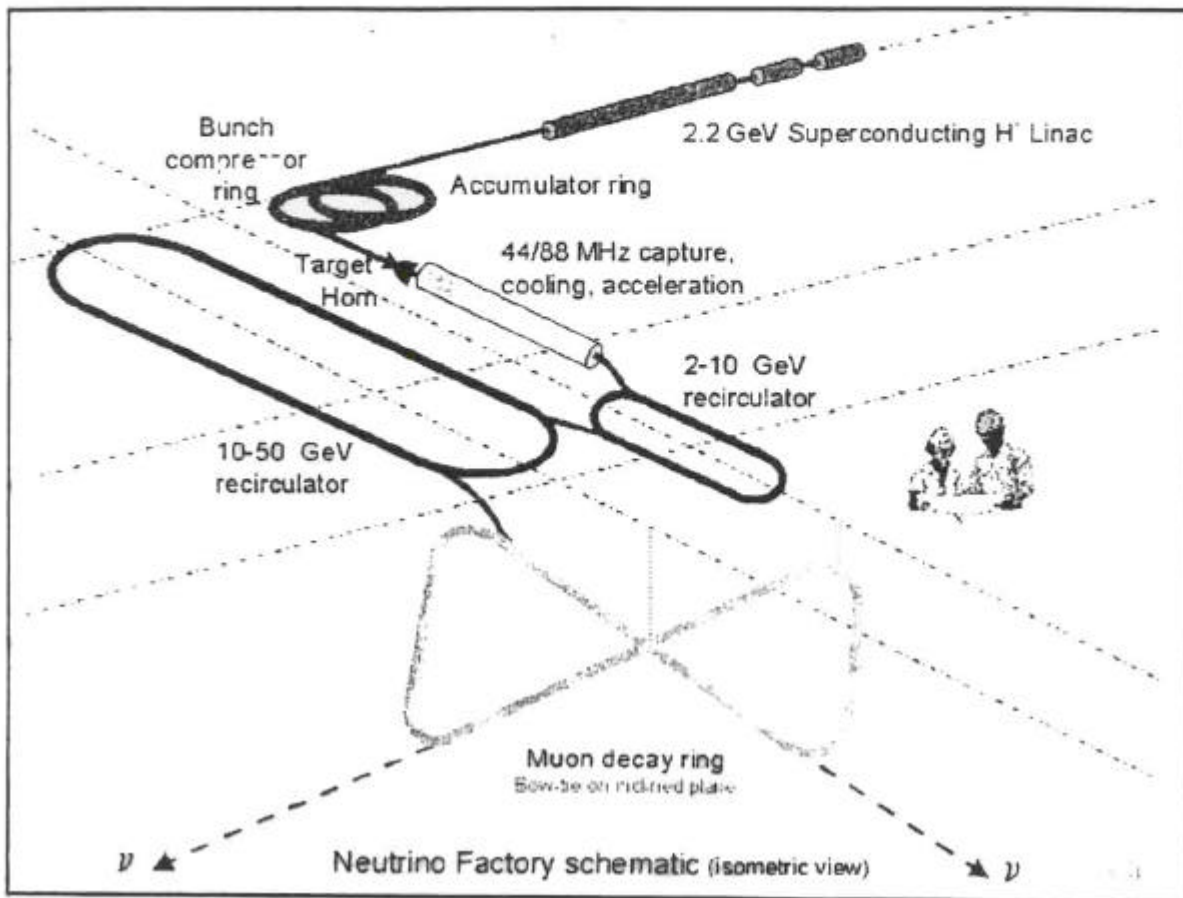
- A. Neutrino Oscillations (F. Dydak, J.J. Gomez-Casas)
- B. High intensity hadron, muon and neutrino beams (J. Ellis)
- B1.  $\nu$  and  $\mu$  DIS (M. Mangano)
- B2. Rare muon decays and muon physics (G. Giudice)
- B3. High intensity Kaon physics (G. Buchalla)

#### Longer-term opportunities opened by the neutrino factory:

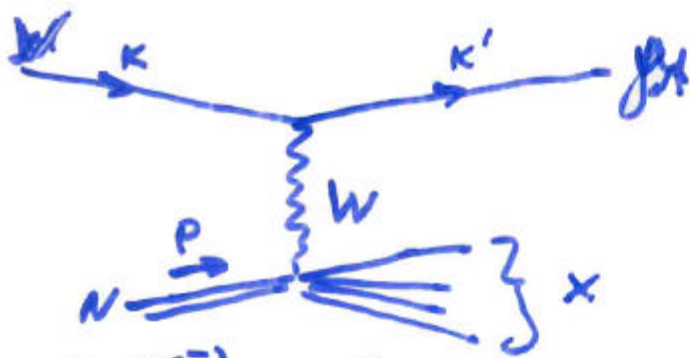
- C. muon colliders, (Marcela Carena, Bill Murray)
- C'. High Energy Frontier  
(coordinated with CLIC studies: J. Ellis/M. Battaglia)

**In parallel with machine design studies by the Neutrino Factory working group mandated by CERN (H. Haseeroth)**

- + High intensity superconducting proton linac (R. Garoby)
- + Rapid cycling synchrotron and accumulator (H. Schonauer)







$$\frac{d^2\sigma^{(\nu\bar{\nu})}}{dx dy} = \frac{G_F^2 M_N E_\nu}{\pi(1+Q^2/M_W^2)^2} \left[ \frac{1}{2} y^2 2x F_1^{(\nu\bar{\nu})} + \left(1-y-\frac{M_N xy}{2E_\nu}\right) F_2^{(\nu\bar{\nu})} \pm (y - \frac{1}{2}y^2) x F_3^{(\nu\bar{\nu})} \right]$$

$$y = \frac{E_{had}}{E_\nu}$$

$$x = \frac{Q^2}{2M_N E_{had}}$$

$$0 < x \leq 1$$

$$\left| \frac{1}{1 + \frac{x M_N}{2E_\nu}} \right| \Rightarrow y \approx 1$$

← not small!  
y

Both  $x F_3$  and  $x F_1$  may be extracted!

Usually extracted:  $x F_3, F_2, R = \frac{\sigma_L}{\sigma_T} = \left(1 + \frac{4M_N^2 x}{Q^2}\right) x \frac{F_2}{2xF_1} - 1$

Another way:

$$F_1^{(\nu N)} = \frac{F_2^{(\nu N)}}{2x} + \frac{F_L^{(\nu N)}}{2x}$$

So instead of fits of  $R, F_2^{(\nu\bar{\nu})}, x F_3^{(\nu\bar{\nu})}$

6-parameters:  $2xF_1^{\bar{\nu}}, 2xF_1^{\nu}, F_2^{\bar{\nu}}, F_2^{\nu}, xF_3^{\bar{\nu}}, xF_3^{\nu}$

All available preliminary results:

CCFR (Iron)

CHORUS (R. Oldeman, Thesis)  
Lead

EW-corrections D. Bardin, Doluckaev. (86)  
NUDIS1 -  $\frac{d\sigma}{dx}$   
NUDIS2  $\rightarrow \frac{d\sigma}{dx dy}$

⑤

## Theoretical QCD Kitcher

DGLAP equation

$$Q^2 \frac{d}{dQ^2} F_3(x, Q^2) = \frac{1}{x} \int_x^1 \frac{dy}{y} \left[ V_{F_3}(y, A_s) + \beta(A_s) \frac{\partial \ln C_{F_3}^{(A_s)}}{\partial A_s} \right] F_3\left(\frac{x}{y}, Q^2\right)$$

$$Q^2 \frac{\partial A_s}{\partial Q^2} = \beta(A_s) = - \sum_{i=0}^2 \beta_i A_s^{i+2}; \quad A_s = \frac{d_s}{4\pi}$$

$\beta(A_s)$  is calculated at 4-loops - NNLO

Ritbergen, Vermaseren, Larin (97)

$$C_{F_3}(y, A_s) = \sum_{n=0}^2 C_{F_3, n} A_s^{n^2}$$

calculated to  $A_s^2$  van Neerven, Zijlstra (91)

$$V_{F_3}(z, d_s) = \sum_{n=0}^2 V_n(z) A_s^{n+1}, \text{ calculated at } A_s^2$$

$V_3(z)$  - model - new

van Neerven, Vogt (01)

Moments

$$\int_0^1 z^{n-1} V_{F_3}(z, A_s) = \sum_{i=0}^2 \gamma_{F_3}^{(i)}(n) A_s^{i+1}$$

$\gamma_{F_3}^{(2)}(n)$  - 3 loops calculated analytically  
at  $n=3, 5, 7, 9, 11, 13$   $\Rightarrow$  NNLO

Retey, Vermaseren (00)

$$\int_0^1 z^n F_3(z, A_s) = \sum_{i=0}^3 C^{(i)}(n) A_s^{i+1}$$

NNLO  $C^{(2)}(n)$  - calculated analytically at any  $n$ .

NNLO  $C^{(3)}(n)$  - calculated analytically at  
 $n=1, 3, 5, 7, 9, 11, 13$

Retey, Vermaseren (00)

⑥

## Method of the fits.

Jacobi polynomial technique

$$F_3(x, Q^2) = x^\alpha (1-x)^\beta \sum_{n=0}^{N_{\max}} O_n(\alpha) \sum_j C_j^{(n)}(\alpha, \beta) x^j \times M_{j+2, x} F_3(Q^2)$$

$$M_{j+2, x} F_3(Q^2) = \int_0^1 x^{j+2} F_3(x, Q^2) dx$$

In the process of

NNLO fits: NNLO  $\beta(\alpha_s)$ ,  $\gamma_{F_3}(\alpha_s)$ ,  $C_{F_3}^{(2)}$   
N<sup>3</sup>LO fits: N<sup>3</sup>LO  $\beta(\alpha_s)$ ,  $C_{F_3}^{(2)}$ ,  $\gamma_{F_3}$  - Padé

weaker sensitivity

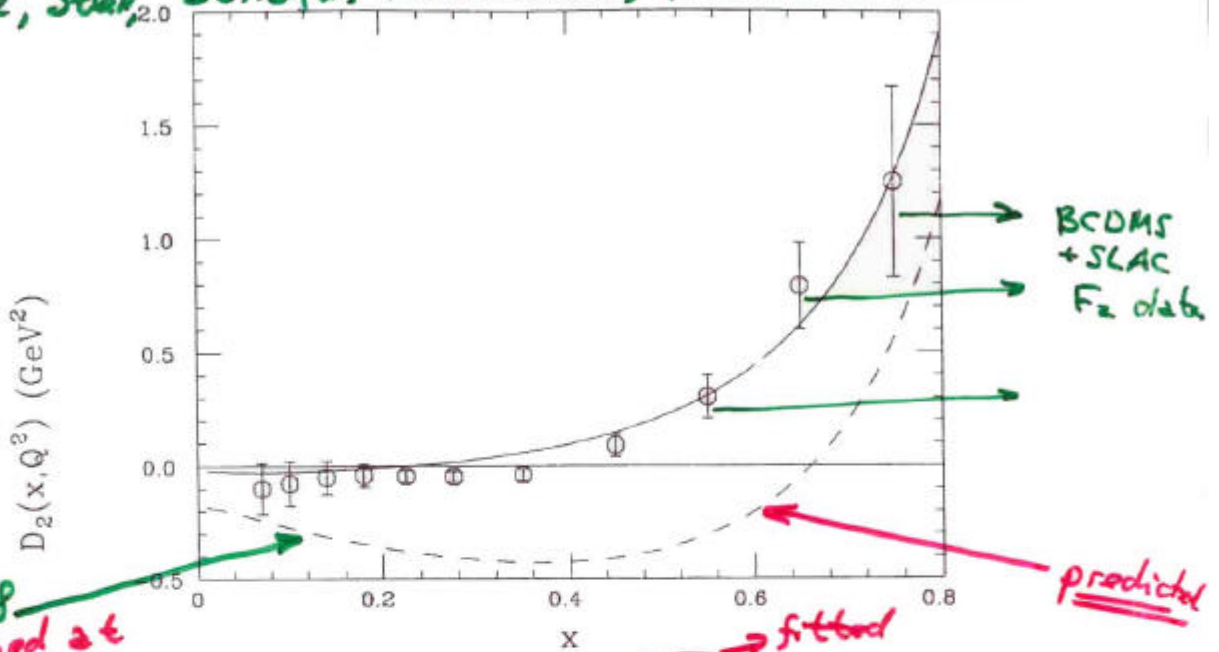
Determination:  $\Lambda_{\overline{MS}}^{(4)} \rightarrow d_s(Q^2) \rightarrow d_s(M_Z)$



⑦

Why extraction of  $x F_3$  is interesting?

Dasgupta, Webber, PL B 382 (1996) 273  
 Maul, Stein, Schäfer, Montkiewicz, PL B 401 (97) 100



KKPS '98 confirmed at NLO from CCFR '97 fits

Figure 1: Coefficients of  $1/Q^2$  contributions to  $F_2$  (solid) and to  $F_1$  and  $F_3$  (dashed).

For  $F_1$  and  $F_3$   $D_i(x)$  is the same!

$$F_i(x, Q^2) = F_i(x, Q^2) \left[ 1 + \frac{D_2^{(i)}(x)}{Q^2} + O\left(\frac{1}{Q^4}\right) \right]$$

$$D_2^{(2)}(x) \sim \frac{A_2'}{q(x, Q^2)} \int \frac{dz}{z} C_2(z) q(x/z, Q^2)$$

parton distribution

$C_2(x)$  → calculated from set of diagrams



Infrared renormalon model

$$\text{red circle} \equiv \text{green circle} + \text{green circle with gluon} + \text{green circle with gluon} + \dots$$

generate  $\frac{1}{Q^2}$  - correction after resummation

8

Fits to CCFR'97 with HT included



order/ $N_{max}$	$Q_0^2 =$	5 GeV <sup>2</sup>	20 GeV <sup>2</sup>	100 GeV <sup>2</sup>
NLO/9 (KPS'01= KPS'00)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'/[\text{GeV}^2]$	<u>379±41</u> 78.6/86 <u>-0.125±0.053</u>	<u>376±39</u> 79.5/86 <u>-0.125±0.053</u>	<u>374±42</u> 79.0 <u>-0.124±0.053</u>
NNLO/6 (KPS'01)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'/[\text{GeV}^2]$	297±30 77.9/86 -0.007±0.051	<b>328±36</b> <b>76.8/86</b> <b>-0.017±0.051</b>	328±35 79.5 -0.015±0.051
NNLO/6 (KPS'00)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'/[\text{GeV}^2]$	- - -	<b>326±35</b> <b>76.9/86</b> <b>-0.01±0.05</b>	- - -
NNLO/9 (KPS'01)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'/[\text{GeV}^2]$	<b>331±33</b> <b>73.1/86</b> <b>-0.013±0.051</b>	<b>332±35</b> <b>75.7/86</b> <b>-0.015±0.051</b>	<b>331±35</b> <b>76.9/86</b> <b>-0.016±0.051</b>
N <sup>3</sup> LO/6 (KPS'01)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'/[\text{GeV}^2]$	305±29 76.0/86 0.036±0.051	327±34 76.2/86 0.033±0.052	326±34 78.5 0.029±0.052
Padé/6 (KPS'00)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'$	- - -	340±37 77.2/86 -0.004±0.05	- - -
N <sup>3</sup> LO/9 (KPS'01)	$\Lambda_{\overline{MS}}^{(4)}/[\text{MeV}]$ $\chi^2/\text{nep}$ $A_2'/[\text{GeV}^2]$	<b>333±34</b> <b>73.8/86</b> <b>0.038±0.052</b>	<b>328±33</b> <b>75.9/86</b> <b>0.035±0.052</b>	<b>328±38</b> <b>76.4/86</b> <b>0.034±0.052</b>

At  $N_{max}=9 \Rightarrow$  Stability to  $Q_0^2$  !!  $\chi^2$  is minimized

$$\frac{h(x)}{Q^2} = x^\alpha (1-x)^\beta \sum_{n=0}^{N_{max}} \Theta_n^{\alpha, \beta}(x) \sum_{j=0}^n C_j^{(n)}(\alpha, \beta) M_{j+2, xF_j}^{IRR}(Q^2)$$

$$M_{n, xF_j}^{IRR}(Q^2) = \tilde{C}(n) M_n^F(Q^2) \frac{A_c^I}{Q^2}$$

$$\tilde{C}(n) = -n - 4 + \frac{2}{n+1} + \frac{4}{n+2} + 4 \sum_{j=1}^n \frac{1}{j}$$

- At NLO  $\Rightarrow$  one can extract  $A_c^I$  and  $\Lambda_{\overline{MS}}^{(4)}$
  - Starting from NNLO  $\Rightarrow A_c^I$  is "screened" by higher order terms
- May be CCFR'97 data are not so precise?  $\Rightarrow$  or general feature?



9 Notice, that interplay of HT and NNLO order corrections exist in the case of another model

SY'01 used (Santiago, Yndurain)

M\_{n,IF\_3}^{HT}(Q^2) = n \frac{B'\_2}{Q^2} M\_n^{F\_3}(Q^2), with B'\_2 = a(\Lambda\_{\overline{MS}}^{(4)})^2

only in the NNLO fits

KPS'01 results: (Jacobi)

Table with 6 columns: Order, Lambda\_MS^(4), chi^2/nep, B'\_2, a, alpha\_s(M\_Z). Rows: LO, NLO, NNLO.

in agreement with SY'01

We noticed, that the observed feature of HT-duality (or interplay between NNLO and HT/Q^2 - corrections is model independ

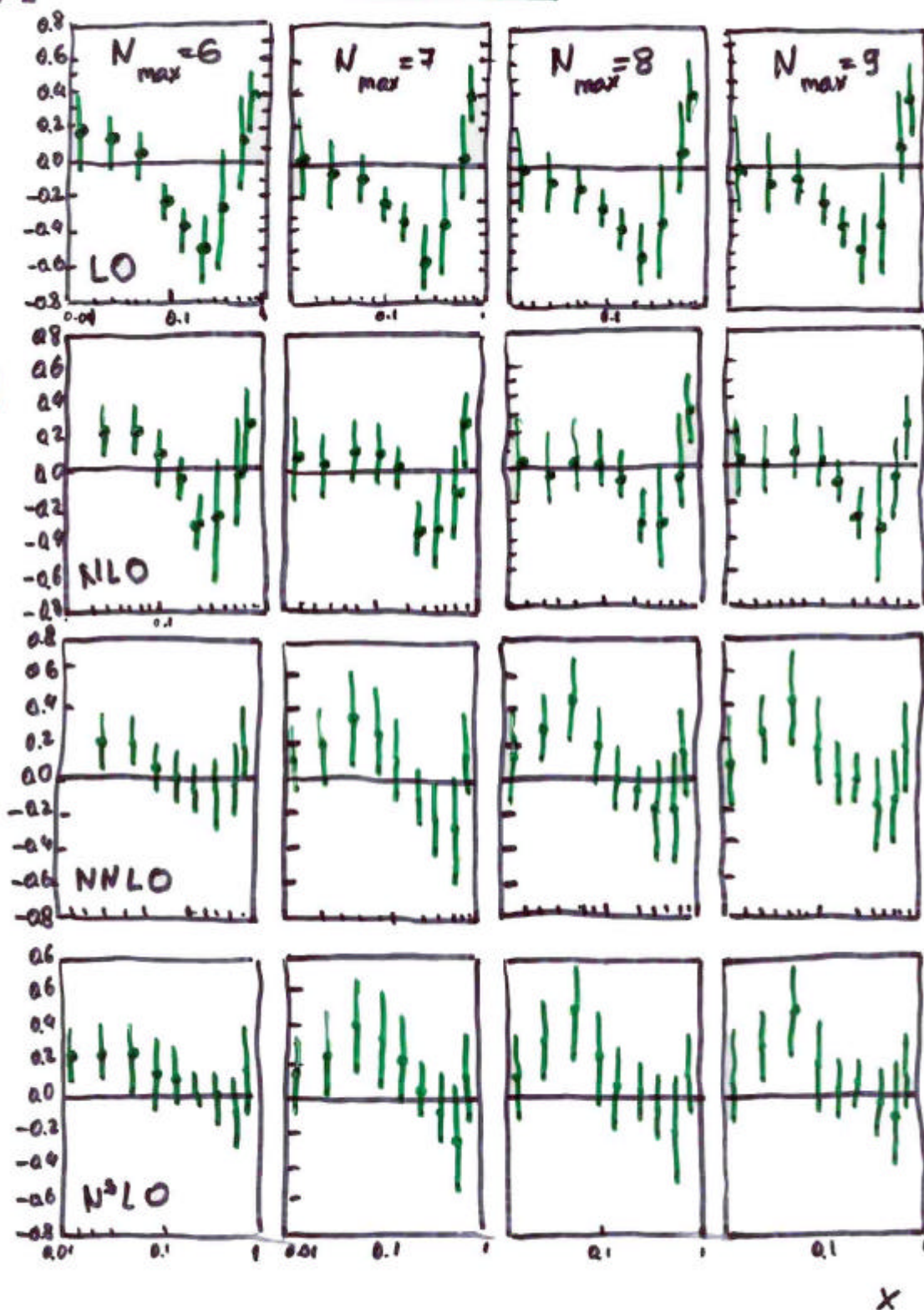
|B'\_2|\_{LO} > |B'\_2|\_{NLO} > |B'\_2|\_{NNLO}

In agreement with original observation - KKPS'98; KPS'01

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# Interplay between perturbative and high-twist corrections

$h(x)$   
[GeV<sup>2</sup>]



Kataev, Parente, Sidorov (01)



12

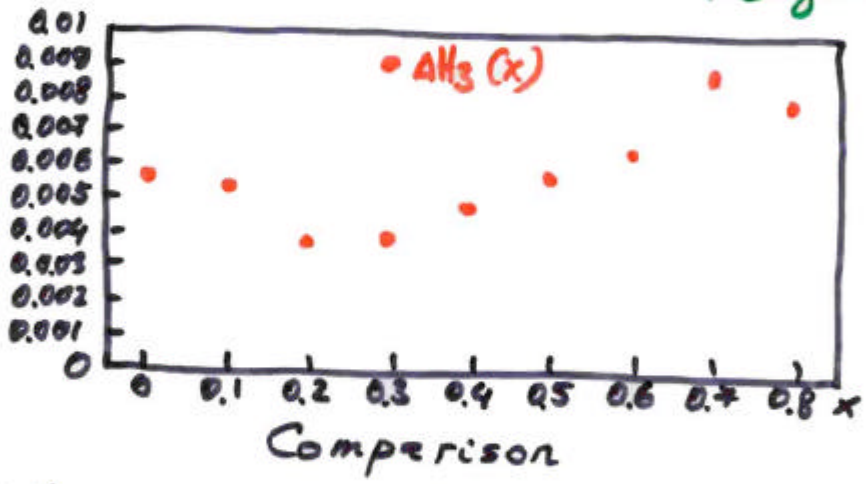
At NNLO and N<sup>3</sup>LO effects of HT less vivid

(\*) Interplay between HO perturbative corrections or (\*\*) lack of precision of CCFR '97 Tevatron data for  $xF_3$  ?

At Neutrino factory this problem can be clarified: increase of precision of  $xF_3$  data

$$F_3(x, Q^2) = F_3^{LT}(x, Q^2) + \frac{H(x)}{Q^2}$$

Mangano et al (04)



IRR - model parameter

$$H(x) = -\frac{2CF_A^2}{\beta_0} \int_x^1 dz C(z) F_3^{LT}(x/z, Q)$$

Experiment	$\Lambda_s^2$ (GeV <sup>2</sup> )
IHEP-JINR	$0.69 \pm 0.33$
CCFR	$0.36 \pm 0.22$
VF-	$\pm 0.00?$

NLO fits.

At Neutrino Factory data expected drastically more precis

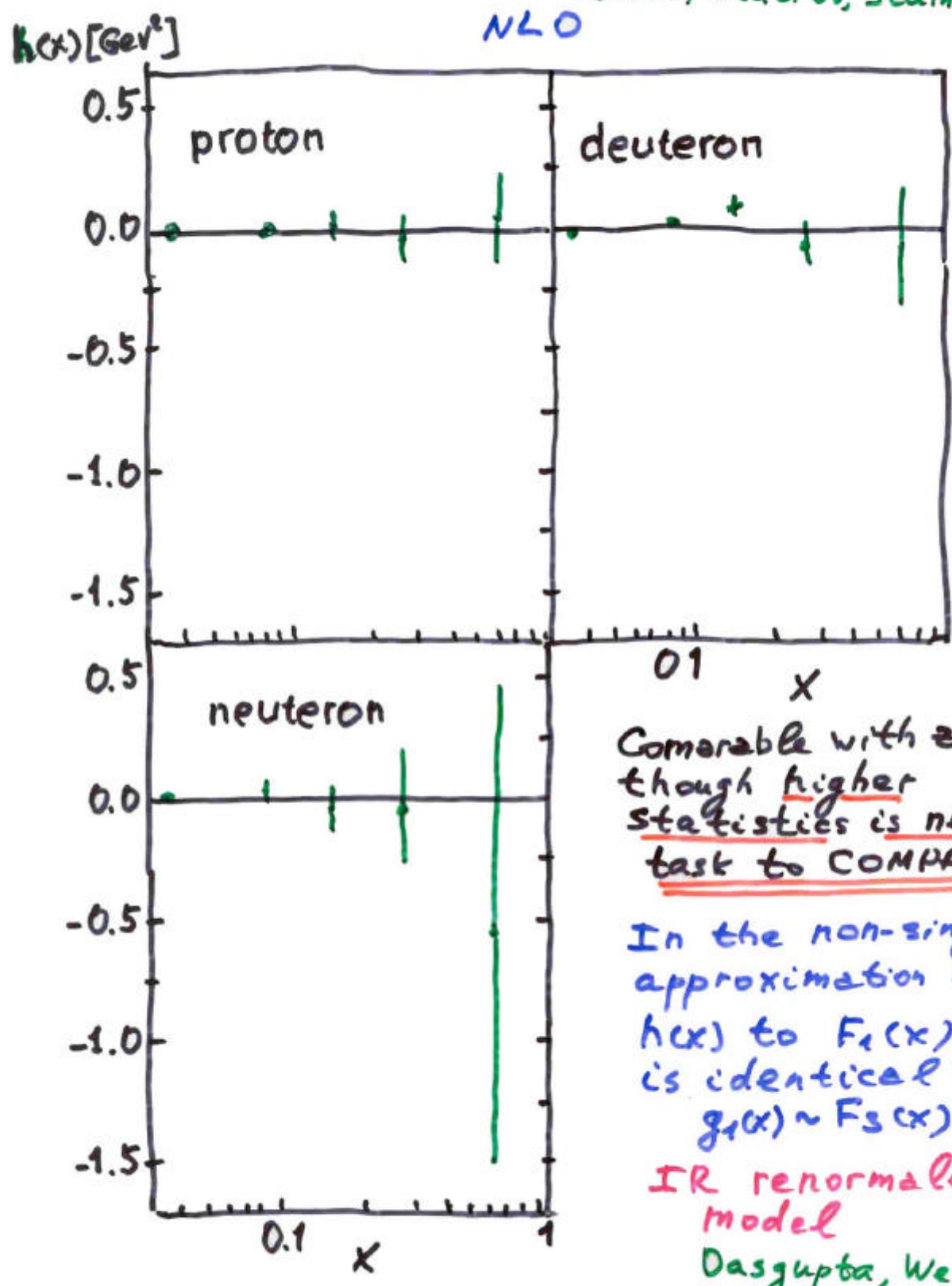


12

HT corrections to  $A_1 = (1+\gamma^2) \frac{g_1}{F_1} + \frac{h(x)}{Q^2}$

Leader, Sidorov, Stamenov(α)

NLO



Comparable with zero, though higher statistics is needed task to COMPASS

In the non-singlet approximation  $x > 0.2$   $h(x)$  to  $F_2(x)$  is identical to  $g_1(x) \sim F_3(x)$

IR renormalon model

Dasgupta, Webber

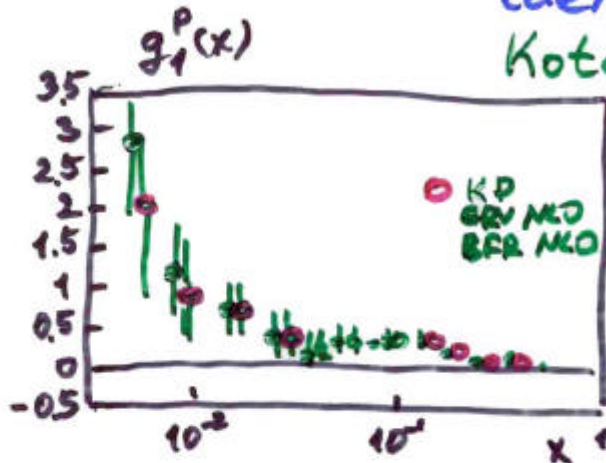
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## Limitation to $g_1(x)$ analysis at NLO

① NS approximation

$g_1(x) \approx F_3(x)$ ; NLO evolution is identical to  $x F_3$

Kotikov, Peshekhonov (01)



Ball, Forte, Ridolfi  
Good agreement  
However, no information  
on SI contribution  
to  $g_1(x)$  (KP)

②  $x F_3$  and  $g_1(x)$

Coefficient functions are known at NLO

van Neerven, Zijlstra (92)

DGLAP kernel

NLO mode exist for  $x F_3$

No  $g_1(x)$

③ Precision of  $g_1(x)$  experimentally not so good, in particular at small  $x \Rightarrow$  COMPASS

More precise data at moderate  $Q^2$  - Neutrino Factory

[These possible new data provide possibility to study HT effects to  $g_1(x)$  and  $x F_3$ ]